

# Orange Public Schools

Office of Curriculum & Instruction  
2019-2020 Mathematics Curriculum Guide



## Fourth Grade

Eureka - Module 6: Decimal Fractions

*March 9, 2020 – April 9, 2020*

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## Yearlong Pacing Guide: Second Grade

<b><i>Eureka Math</i></b>	<b><i>Eureka Module Standards</i></b>
Unit 1- Module 1: Place Value, Round, and Algorithms for Addition/ Subtraction <b>Sept 9- Oct 18</b>	<b>4OA3, 4NBT1, 4NBT2,</b> <b>4NBT3, 4NBT4</b>
Unit 2- Module 3: Multi-Digit Multiplication and Division <b>Oct 21- Dec 20</b>	<b>4OA1, 4OA2, 4OA3, 4OA4,</b> <b>4NBT5, 4NBT6, 4MD3</b>
Unit 3- Module 5: Fractions Equivalence, Ordering, and Operations <b>Jan 2- March 6</b>	<b>4NF1,4NF2, 4NF3,</b> <b>4NF4, 4MD4</b>
Unit 4- Module 6: Decimal Fractions <b>March 9- April 9</b>	<b>4NF5,4NF6, 4NF7,4MD2</b>
Unit 5- Module 4: Angle Measures and Plane Figures <b>April 20- May 15</b>	<b>4MD5, 4MD6, 4MD7,</b> <b>4G1, 4G2, 4G3</b>
Unit 6- Module 2: Unit Conversions and Problem Solving <b>May 18- May 29</b>	<b>4.MD.1, 4.MD.2</b>
Unit 7- Module 7: Exploring Multiplication <b>June 1- EOSY</b>	<b>4OA1, 4OA2, 4OA3, 4MD1,</b> <b>4.NBT5, 4.NBT6 4MD2</b>

### References

“Eureka Math” *Gt Minds*. 2018 < <https://greatminds.org/account/product>

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## Module 6

### Essential Questions

### Enduring Understandings

- |   |   |
|---|---|
| <ul style="list-style-type: none"> <li>• How can visual models be used to help with understanding decimals?</li> <li>• How can visual models be used to determine and compare equivalent fractions and decimals?</li> <li>• How would you compare and order decimals through hundredths?</li> </ul> | <ul style="list-style-type: none"> <li>• Fractions with denominators of 10 can be expressed as an equivalent fraction with a denominator of 100.</li> <li>• Fractions with denominators of 10 and 100 may be expressed using decimal notation.</li> <li>• When comparing two decimals to hundredths, the comparisons are valid only if they refer to the same whole.</li> </ul> |
|---|---|

## Performance Overview

- In Topic A, students use their understanding of fractions to explore tenths. Students use metric measurement and see tenths in relation to one whole in the context of 1 kilogram, 1 meter, and 1 centimeter. Through further exploration and observation of a digital scale, students learn that  $\frac{1}{10}$  kilogram can also be expressed as 0.1 kilogram, that  $\frac{2}{10}$  kilogram can be expressed as 0.2 kilogram, and that all expressions of tenths in fraction form (up to one whole) can be expressed in decimal form as well.
- In Topic B, students decompose tenths into 10 equal parts to create hundredths. Students also further extend their use of the number line to show the ones, tenths, and hundredths as lengths.
- The focus of Topic C is comparison of decimal numbers. Students compare pairs of decimal numbers representing lengths, masses, or volumes by recording them on the place value chart and reasoning about which measurement is longer than (shorter than, heavier than, lighter than, more than, or less than) the other. Comparing decimals in the context of measurement supports their justifications of their conclusions and begins their work with comparison at a more concrete level.
- Topic D brings together students' work with addition of fractions and their work with decimals. They progress to using multiplication to generate equivalent fractions and express the sum in fraction form as a decimal. Students next apply what they know about fraction addition to use multiple strategies to solve sums of tenths and hundredths with totals greater than 1, again expressing the solution in decimal form.
- In Topic E, students work with money amounts as decimal numbers, applying what they have come to understand about decimals. They apply their understanding of tenths and hundredths to express money amounts in both fraction and decimal forms. They solve word problems involving money using all four operations. Addition and subtraction word problems are computed using dollars and cents in unit form. Multiplication and division word problems are computed using cents in unit form. All answers are converted from unit form into decimal form, using the dollar symbol as the unit.

Module 6: Decimal Fractions**Pacing:**

March 9, 2020- April 9, 2020

Suggested Instructional Days: 22

Topic	Lesson	Lesson Objective/ Supportive Videos
<b>Topic A:</b> Exploration of Tenths	Lesson 1	Use metric measurement to model the decomposition of one whole into tenths. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 2	Use metric measurement and area models to represent tenths as fractions greater than 1 and decimal numbers. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 3	Represent mixed numbers with units of tens, ones, and tenths with number disks, on the number line, and in expanded form. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 5	Model the equivalence of tenths and hundredths using the area model and number disks. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 6	Use the area model and number line to represent mixed numbers with units of ones, tenths, and hundredths in fraction and decimal forms. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 7	Model mixed numbers with units of hundreds, tens, ones, tenths, and hundredths in expanded form and on the place value chart. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 8	Use understanding of fraction equivalence to investigate decimal numbers on the place value chart expressed in different units. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
<b>Mid Module Assessment</b>		
<b>Topic C:</b> Decimal Comparison	Lesson 9	Use the place value chart and metric measurement to compare decimals and answer comparison questions. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 10	Use area models and the number line to compare decimal numbers, and record comparisons using $<$ , $>$ , and $=$ . <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 11	Compare and order mixed numbers in various forms. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>

<b>Topic D:</b> Addition with Tenths and Hun- dredths	Lesson 12	Apply understanding of fraction equivalence to add tenths and hundredths. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 13	Add decimal numbers by converting to fraction form. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 14	Solve word problems involving the addition of measurements in decimal form. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
<b>Topic E:</b> Money Amounts as Decimal Numbers	Lesson 15	Express money amounts given in various forms as decimal numbers. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
	Lesson 16	Solve word problems involving money. <a href="https://www.youtube.com/watch?v">https://www.youtube.com/watch?v</a>
<b>End of Module Assessment</b>		

<b>Modifications</b>	
<b>Special Education/ 504:</b>	<b>English Language Learners:</b>
<ul style="list-style-type: none"> <li>-Adhere to all modifications and health concerns stated in each IEP.</li> <li>-Give students a menu of options, allowing students to pick assignments from different levels based on difficulty.</li> <li>-Accommodate Instructional Strategies: reading aloud text, graphic organizers, one-on-one instruction, class website (Google Classroom), handouts, definition list with visuals, extended time</li> <li>-Allow students to demonstrate understanding of a problem by drawing the picture of the answer and then explaining the reasoning orally and/or in writing, such as Read-Draw-Write</li> <li>-Provide breaks between tasks, use positive reinforcement, use proximity</li> <li>-Assure students have experiences that are on the Concrete- Pictorial- Abstract spectrum by using manipulatives</li> <li>-Common Core Approach to Differentiate Instruction: Students with Disabilities (<a href="#">pg 17-18</a>)</li> <li>- <a href="#">Strategies for Students with 504 Plans</a></li> </ul>	<ul style="list-style-type: none"> <li>- Use manipulatives to promote conceptual understanding and enhance vocabulary usage</li> <li>- Provide graphic representations, gestures, drawings, equations, realia, and pictures during all segments of instruction</li> <li>- During i-Ready lessons, click on “Español” to hear specific words in Spanish</li> <li>- Utilize graphic organizers which are concrete, pictorial ways of constructing knowledge and organizing information</li> <li>- Use sentence frames and questioning strategies so that students will explain their thinking/ process of how to solve word problems</li> <li>- Utilize program translations (if available) for L1/ L2 students</li> <li>- Reword questions in simpler language</li> <li>- Make use of the ELL Mathematical Language Routines (click <a href="#">here</a> for additional information)</li> <li>-Scaffolding instruction for ELL Learners</li> <li>-Common Core Approach to Differentiate Instruction: Students with Disabilities (<a href="#">pg 16-17</a>)</li> </ul>
<b>Gifted and Talented:</b>	<b>Students at Risk for Failure:</b>
<ul style="list-style-type: none"> <li>- Elevated contextual complexity</li> <li>- Inquiry based or open ended assignments and projects</li> <li>- More time to study concepts with greater depth</li> <li>- Promote the synthesis of concepts and making real world connections</li> <li>- Provide students with enrichment practice that are imbedded in the curriculum such as:                             <ul style="list-style-type: none"> <li>● Application / Conceptual Development</li> <li>● Are you ready for more?</li> </ul> </li> <li>- Common Core Approach to Differentiate Instruction: Students with Disabilities (<a href="#">pg. 20</a>)</li> <li>- Provide opportunities for math competitions</li> <li>- Alternative instruction pathways available</li> </ul>	<ul style="list-style-type: none"> <li>- Assure students have experiences that are on the Concrete- Pictorial- Abstract spectrum</li> <li>- Modify Instructional Strategies, reading aloud text, graphic organizers, one-on-one instruction, class website (Google Classroom), inclusion of more visuals and manipulatives, Field Trips, Google Expeditions, Peer Support, one on one instruction</li> <li>- Assure constant parental/ guardian contact throughout the year with successes/ challenges</li> <li>- Provide academic contracts to students and guardians</li> <li>- Create an interactive notebook with samples, key vocabulary words, student goals/ objectives.</li> <li>- Always plan to address students at risk in your learning tasks, instructions, and directions. Try to anticipate where the needs will be and then address them prior to lessons.</li> <li>-Common Core Approach to Differentiate Instruction: Students with Disabilities (<a href="#">pg 19</a>)</li> </ul>



### 21st Century Life and Career Skills:

Career Ready Practices describe the career-ready skills that all educators in all content areas should seek to develop in their students. They are practices that have been linked to increase college, career, and life success. Career Ready Practices should be taught and reinforced in all career exploration and preparation programs with increasingly higher levels of complexity and expectation as a student advances through a program of study.

<https://www.state.nj.us/education/cccs/2014/career/9.pdf>

- |  |  |
|--|--|
| <ul style="list-style-type: none"><li>● <b>CRP1.</b> Act as a responsible and contributing citizen and employee.</li><li>● <b>CRP2.</b> Apply appropriate academic and technical skills.</li><li>● <b>CRP3.</b> Attend to personal health and financial well-being.</li><li>● <b>CRP4.</b> Communicate clearly and effectively and with reason.</li><li>● <b>CRP5.</b> Consider the environmental, social and economic impacts of decisions.</li><li>● <b>CRP6.</b> Demonstrate creativity and innovation.</li></ul> | <ul style="list-style-type: none"><li>● <b>CRP7.</b> Employ valid and reliable research strategies.</li><li>● <b>CRP8.</b> Utilize critical thinking to make sense of problems and persevere in solving them.</li><li>● <b>CRP9.</b> Model integrity, ethical leadership and effective management.</li><li>● <b>CRP10.</b> Plan education and career paths aligned to personal goals.</li><li>● <b>CRP11.</b> Use technology to enhance productivity.</li><li>● <b>CRP12.</b> Work productively in teams while using cultural global competence.</li></ul> |
|--|--|

**Students are given an opportunity to communicate with peers effectively, clearly, and with the use of technical language. They are encouraged to reason through experiences that promote critical thinking and emphasize the importance of perseverance. Students are exposed to various mediums of technology, such as digital learning, calculators, and educational websites.**

### Technology Standards:

All students will be prepared to meet the challenge of a dynamic global society in which they participate, contribute, achieve, and flourish through universal access to people, information, and ideas.

<https://www.state.nj.us/education/cccs/2014/tech/>

#### 8.1 Educational Technology:

All students will use digital tools to access, manage, evaluate, and synthesize information in order to solve problems individually and collaborate and to create and communicate knowledge.

- A. **Technology Operations and Concepts:** Students demonstrate a sound understanding of technology concepts, systems and operations.
- B. **Creativity and Innovation:** Students demonstrate creative thinking, construct knowledge and develop innovative products and process using technology.
- C. **Communication and Collaboration:** Students use digital media and environments to communicate and work collaboratively, including at a distance, to support individual learning and contribute to the learning of others.
- D. **Digital Citizenship:** Students understand human, cultural, and societal issues related to technology and practice legal and ethical behavior.
- E. **Research and Information Fluency:** Students apply digital tools to gather, evaluate, and use of information.
- F. **Critical thinking, problem solving, and decision making:** Students use critical thinking skills to plan and conduct research, manage projects, solve problems, and make informed decisions using appropriate digital tools and resources.

#### 8.2 Technology Education, Engineering, Design, and Computational Thinking - Programming:

All students will develop an understanding of the nature and impact of technology, engineering, technological design, computational thinking and the designed world as they relate to the individual, global society, and the environment.

- A. **The Nature of Technology: Creativity and Innovation-** Technology systems impact every aspect of the world in which we live.
- B. **Technology and Society:** Knowledge and understanding of human, cultural, and societal values are fundamental when designing technological systems and products in the global society.
- C. **Design:** The design process is a systematic approach to solving problems.
- D. **Abilities in a Technological World:** The designed world in a product of a design process that provides the means to convert resources into products and systems.
- E. **Computational Thinking: Programming-** Computational thinking builds and enhances problem solving, allowing students to move beyond using knowledge to creating knowledge.

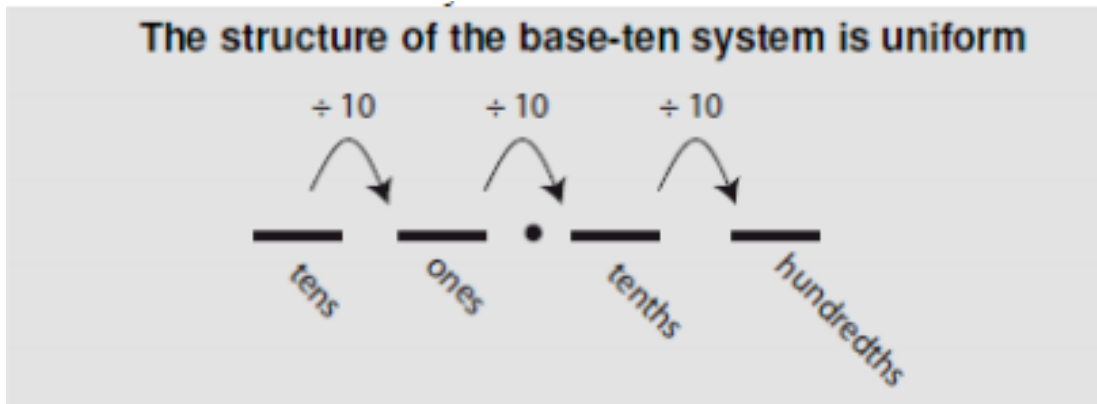
<b>Interdisciplinary Connections:</b>	
<b>English Language Arts:</b>	
RF.4.4	Read with sufficient accuracy and fluency to support comprehension.
W.4.10	Write routinely over extended time frames (time for research, reflection, and revision) and shorter time frames (a single sitting or a day or two) for a range of discipline-specific tasks, purposes, and audiences.
SL.4.1	Engage effectively in a range of collaborative discussions (one-on-one, in groups, and teacher-led) with diverse partners on <i>grade 4 topics and texts</i> , building on others' ideas and expressing their own clearly.

### NJSLS Unpacked Standards

**4.NF.5**

Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100.<sup>2</sup>For example, express  $3/10$  as  $30/100$ , and add  $3/10 + 4/100 = 34/100$ .

- This standard continues the work of equivalent fractions by having students change fractions with a 10 in the denominator into equivalent fractions that have a 100 in the denominator.
- In order to prepare for work with decimals (4.NF.6 and 4.NF.7), experiences that allow students to shade decimal grids (10x10 grids) can support this work. Student experiences should focus on working with grids rather than algorithms.
- Students can also use base ten blocks and other place value models to explore the relationship between fractions with denominators of 10 and denominators of 100.
- Students in fourth grade work with fractions having denominators 10 and 100. Because it involves partitioning into 10 equal parts and treating the parts as numbers called one tenth and one hundredth, work with these fractions can be used as preparation to extend the base-ten system to non-whole numbers.

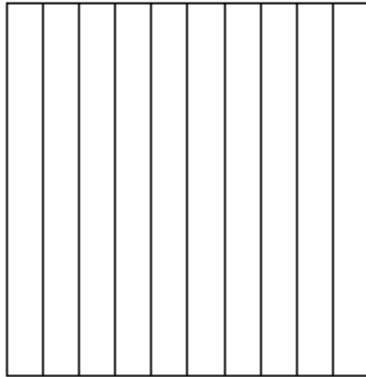


- This work in fourth grade lays the foundation for performing operations with decimal numbers in fifth grade.

**Example:**

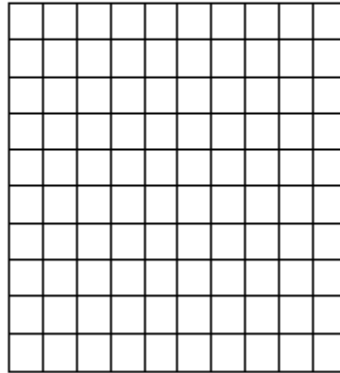
<b>Ones</b>	<b>.</b>	<b>Tenths</b>	<b>Hundredths</b>
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**Tenths Grid**



**.3 = 3 tenths = 3/10**

**Hundredths Grid**

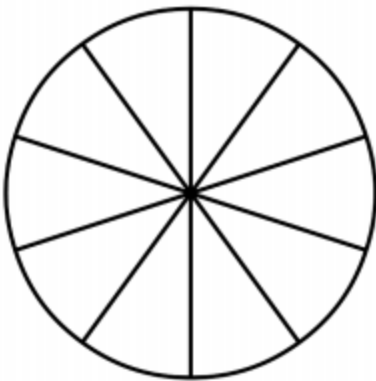


**.30 = 30 hundredths = 30/100**

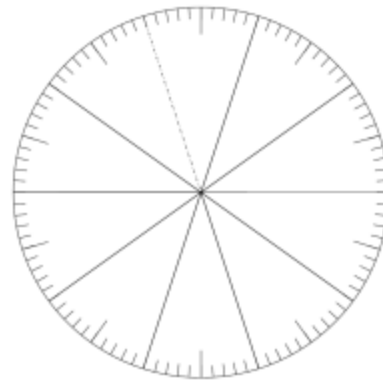
**Example:**

Represent 3 tenths and 30 hundredths on the models below.

10<sup>th</sup>s circle



100<sup>th</sup>s circle



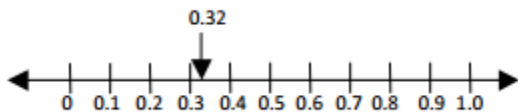
4.NF.6

Use decimal notation for fractions with denominators 10 or 100. For example, rewrite  $0.62$  as  $62/100$ ; describe a length as  $0.62$  meters; locate  $0.62$  on a number line diagram.

- Decimals are introduced for the first time. Students should have ample opportunities to explore and reason about the idea that a number can be represented as both a fraction and a decimal.
- Students make connections between fractions with denominators of 10 and 100 and the place value chart. By reading fraction names, students say  $32/100$  as thirty-two hundredths and rewrite this as  $0.32$  or represent it on a place value model as shown below.

Hundreds	Tens	Ones	•	Tenths	Hundredths
			•	3	2

- Students represent values such as  $0.32$  or  $32/100$  on a number line.  $32/100$  is more than  $30/100$  (or  $3/10$ ) and less than  $40/100$  (or  $4/10$ ). It is closer to  $30/100$  so it would be placed on the number line near that value.



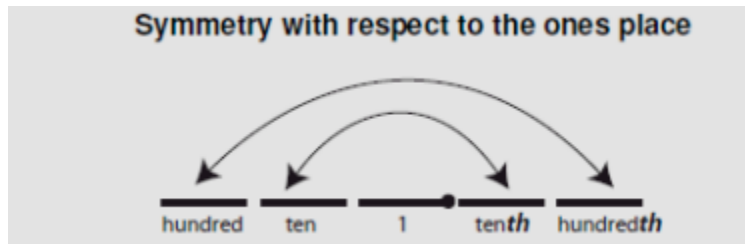
4.NF.7

Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols  $>$ ,  $=$ , or  $<$ , and justify the conclusions, e.g., by using a visual model.

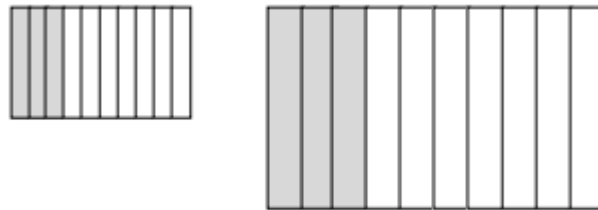
- Students should reason that comparisons are only valid when they refer to the same whole. Visual models include area models, decimal grids, decimal circles, number lines, and meter sticks.
- The decimal point is used to signify the location of the ones place, but its location may suggest there should be a "oneths" place to its right in order to create symmetry with respect to the decimal point. However, because one is the basic unit from which the other base ten units are derived, the symmetry occurs instead with respect to the ones place.
- Ways of reading decimals aloud vary. Mathematicians and scientists often read  $0.15$  aloud as "zero point one five" or "point one five." (Decimals smaller than one may be written with or without a zero before the decimal point.) Decimals with many non-zero digits are more easily read aloud in this manner. (For example, the number  $\pi$ , which has infinitely many non-zero digits, begins  $3.1415 \dots$ )
- Other ways to read  $0.15$  aloud are "1 tenth and 5 hundredths" and "15 hundredths," just as  $1,500$  is sometimes read "15 hundred" or "1 thousand, 5 hundred." Similarly,  $150$  is read "one hundred and fifty" or "a hundred fifty" and understood as 15 tens, as 10 tens and 5 tens, and as  $100 + 50$ . Just as  $15$  is understood as 15 ones and as 1 ten and 5 ones in computations with whole numbers,  $0.15$  is viewed as 15 hundredths and as 1 tenth and 5 hundredths in

computations with decimals. It takes time to develop understanding and fluency with the different forms.

- Layered cards for decimals can help students become fluent with decimal equivalencies such as three tenths is thirty hundredths.



- Students build area and other models to compare decimals. Through these experiences and their work with fraction models, **they build the understanding that comparisons between decimals or fractions are only valid when the whole is the same for both cases.**
- Each of the models below shows  $3/10$  but the whole on the right is much bigger than the whole on the left. They are both  $3/10$  but the model on the right is a much larger quantity than the model on the left.



- When the wholes are the same, the decimals or fractions can be compared.

**Example:**

Draw a model to show that  $0.3 < 0.5$ .

(Students would sketch two models of approximately the same size to show the area that represents three-tenths is smaller than the area that represents five-tenths.)



**4.MD.2**

Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.

- This standard includes multi-step word problems related to expressing measurements from a larger unit in terms of a smaller unit (e.g., feet to inches, meters to centimeter, and dollars to cents). Students should have ample opportunities to use number line diagrams to solve word problems.

**Example:**

Charlie and 10 friends are planning for a pizza party. They purchased 3 quarts of milk. If each glass holds 8oz will everyone get at least one glass of milk?

*Possible solution:*

Charlie plus 10 friends = 11 total people

11 people x 8 ounces (glass of milk) = 88 total ounces

1 quart = 2 pints = 4 cups = 32 ounces

Therefore 1 quart = 2 pints = 4 cups = 32 ounces

2 quarts = 4 pints = 8 cups = 64 ounces

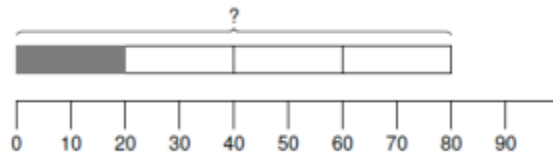
3 quarts = 6 pints = 12 cups = 96 ounces

If Charlie purchased 3 quarts (6 pints) of milk there would be enough for everyone at his party to have at least one glass of milk. If each person drank 1 glass then he would have 1- 8 oz glass or 1 cup of milk left over.

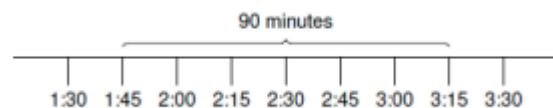
**Additional Examples with various operations:**

- *Division/fractions:* Susan has 2 feet of ribbon. She wants to give her ribbon to her 3 best friends so each friend gets the same amount. How much ribbon will each friend get? Students may record their solutions using fractions or inches. (The answer would be  $\frac{2}{3}$  of a foot or 8 inches. Students are able to express the answer in inches because they understand that  $\frac{1}{3}$  of a foot is 4 inches and  $\frac{2}{3}$  of a foot is 2 groups of  $\frac{1}{3}$ .)
- *Addition:* Mason ran for an hour and 15 minutes on Monday, 25 minutes on Tuesday, and 40 minutes on Wednesday. What was the total number of minutes Mason ran?
- *Subtraction:* A pound of apples costs \$1.20. Rachel bought a pound and a half of apples. If she gave the clerk a \$5.00 bill, how much change will she get back?
- *Multiplication:* Mario and his 2 brothers are selling lemonade. Mario brought one and a half liters, Javier brought 2 liters and Ernesto brought 450 milliliters. How many total milliliters of lemonade did the boys have?
- Number line diagrams that feature a measurement scale can represent measurement quantities. Examples include: ruler, diagram marking off distance along a road with cities at various points, a timetable showing hours throughout the day, or a volume measure on the side of the container.

Juan spent  $\frac{1}{4}$  of his money on a game. The game cost \$20. How much money did he have at first?



What time does Maria have to leave to be at her friend's house by a quarter after 3 if the trip takes 90 minutes?



Using a number line diagram to represent time is easier if students think of digital clocks rather than round clocks. In the latter case, placing the numbers on the number line involves considering movements of the an minute hands.



Fourth Grade Unit 4: Decimal Fraction

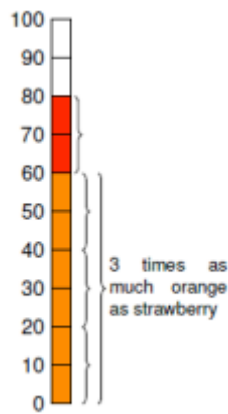
- Students also combine competencies from different domains as they solve measurement problems using all four arithmetic operations, addition, subtraction, multiplication, and division.

**Example:**

“How many liters of juice does the class need to have at least 35 cups if each cup takes 225 ml?” Students may use tape or number line diagrams for solving such problems.

**Example:**

Lisa put two flavors of soda in a glass. There were 80 ml of soda in all. She put three times as much orange drink as strawberry. How many ml of orange did she put in?



**Example:**

At 7:00 a.m. Candace wakes up to go to school. It takes her 8 minutes to shower, 9 minutes to get dressed and 17 minutes to eat breakfast. How many minutes does she have until the bus comes at 8:00 a.m.? Use the number line to help solve the problem.



Common multiplication and division situations.<sup>1</sup>

	<b>UNKNOWN PRODUCT</b>	<b>GROUP SIZE UNKNOWN ("HOW MANY IN EACH GROUP?" DIVISION)</b>	<b>NUMBER OF GROUPS UNKNOWN ("HOW MANY GROUPS?" DIVISION)</b>
	<b><math>3 \times 6 = ?</math></b>	<b><math>3 \times ? = 18</math>, and <math>18 \div 3 = ?</math></b>	<b><math>? \times 6 = 18</math>, and <math>18 \div 6 = ?</math></b>
<b>EQUAL GROUPS</b>	There are 3 bags with 6 plums in each bag. How many plums are there in all? <i>Measurement example.</i> You need 3 lengths of string, each 6 inches long. How much string will you need altogether?	If 18 plums are shared equally into 3 bags, then how many plums will be in each bag? <i>Measurement example.</i> You have 18 inches of string, which you will cut into 3 equal pieces. How long will each piece of string be?	If 18 plums are to be packed 6 to a bag, then how many bags are needed? <i>Measurement example.</i> You have 18 inches of string, which you will cut into pieces that are 6 inches long. How many pieces of string will you have?
<b>ARRAYS<sup>2</sup>, AREA<sup>3</sup></b>	There are 3 rows of apples with 6 apples in each row. How many apples are there? <i>Area example.</i> What is the area of a 3 cm by 6 cm rectangle?	If 18 apples are arranged into 3 equal rows, how many apples will be in each row? <i>Area example.</i> A rectangle has area 18 square centimeters. If one side is 3 cm long, how long is a side next to it?	If 18 apples are arranged into equal rows of 6 apples, how many rows will there be? <i>Area example.</i> A rectangle has area 18 square centimeters. If one side is 6 cm long, how long is a side next to it?
<b>COMPARE</b>	A blue hat costs \$6. A red hat costs 3 times as much as the blue hat. How much does the red hat cost? <i>Measurement example.</i> A rubber band is 6 cm long. How long will the rubber band be when it is stretched to be 3 times as long?	A red hat costs \$18 and that is 3 times as much as a blue hat costs. How much does a blue hat cost? <i>Measurement example.</i> A rubber band is stretched to be 18 cm long and that is 3 times as long as it was at first. How long was the rubber band at first?	A red hat costs \$18 and a blue hat costs \$6. How many times as much does the red hat cost as the blue hat? <i>Measurement example.</i> A rubber band was 6 cm long at first. Now it is stretched to be 18 cm long. How many times as long is the rubber band now as it was at first?
<b>GENERAL</b>	<b><math>a \times b = ?</math></b>	<b><math>a \times ? = p</math> and <math>p \div a = ?</math></b>	<b><math>? \times b = p</math>, and <math>p \div b = ?</math></b>

<sup>1</sup> The language in the array examples shows the easiest form of array problems. A harder form is to use the terms rows and columns: The apples in the grocery window are in 3 rows and 6 columns. How many apples are in there? Both forms are valuable.

<sup>2</sup> Area involves arrays of squares that have been pushed together so that there are no gaps or overlaps, so array problems include these especially important measurement situations.

<sup>3</sup> The first examples in each cell are examples of discrete things. These are easier for students and should be given before the measurement examples.

Module 6 Assessment Framework			
Assessment	NJSLS	Estimated Time	Format
<b>Optional Mid-Module Assessment</b>	4.NF.5-7 4.MD.2	1-2 blocks	Individual
<b>Optional End-of- Module Assessment</b>	4.NF.5-7 4.MD.2	1 Block	Individual or Small Group with Teacher

Module 6 Performance Assessment/ PBL Framework			
Assessment	NJSLS	Estimated Time	Format
<b>Module 6 Performance Task 1</b> <i>Minutes and Days</i>	4.NF.5 4.NF.6	Up to 30 minutes	Individual or Small Group
<b>Extended Constructed Response (ECR)*</b> <a href="#">(click here for access)</a>	Dependent on unit of study & month of administration	Up to 30 Minutes	Individual

Use the following links to access ECR protocol and district assessment scoring documents:

- [Assessment and Data in Mathematics Bulletin](#)
- [ECR Protocol](#)

# Fourth Grade Ideal Math Block

**Fluency: Whole Group**  
Sprints, Counting, Whiteboard Exchange

**Application Problem: Whole Group**  
Provides HANDS-ON work to allow children to ACT OUT or ENGAGE ACTIVELY with the new MATH IDEA  
Technology Integration: <https://embarc.online/>  
\*Website provides Goggle slides, additional activities, and student videos per lesson

**Concept Development: Individual/partner/whole**  
Instruction & Strategic Problem Set Questions  
Technology Integration: <https://embarc.online/>  
Website provides Goggle slides, additional activities, and student videos. per lesson

**Student Debrief: Whole Group**  
Exit Ticket: Independent

**CENTERS/STATIONS:**  
**Pairs / Small Group/ Individual**  
DIFFERENTIATED activities designed to RETEACH, REMEDIATE, ENRICH student's understanding of concepts.

<b>M:</b> Meet with the teacher <a href="https://teacher-toolbox.com/">https://teacher-toolbox.com/</a>	<b>A:</b> Application/ Problem Solving	<b>T:</b> Technology Resources I-ready Zearn	<b>H:</b> Hands on Activities
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50-60 min.

20-30 min.

## Eureka Lesson Structure:

### Fluency:

- Sprints
- Whiteboard Exchange

Technology Integration:

Splat Sequences

[Which one doesn't belong?](#)

[Would you rather?](#)

Esti- Mysteries

### Anchor Task:

- Engage students in using the RDW Process
- Sequence problems from simple to complex and adjust based on students' responses
- Facilitate share and critique of various explanations, representations, and/or examples.

### Guided Practice/ Independent Practice: (largest chunk of time)

Instruction:

- Maintain overall alignment with the objectives and suggested pacing and structure.
- Use of tools, precise mathematical language, and/or models
- Balance teacher talk with opportunities for peer share and/or collaboration
- Generate next steps by watching and listening for understanding

Problem Set: (Individual, partner, or group)

- Allow for independent practice and productive struggle
- Assign problems strategically to differentiate practice as needed
- Create and assign remedial sequences as needed

Technology Integration:

Think Central:

- Pre-Test
- Chapter Review
- Test Prep
- Performance Tasks

<https://embarc.online/>

[Virtual Manipulatives](#) for lessons

<http://nlvm.usu.edu/en/nav/vlibrary.html>

For videos that students can watch and interact with independently click [here](#)

### Student Debrief:

- Elicit students thinking, prompt reflection, and promote metacognition through student centered discussion
- Culminate with students' verbal articulation of their learning for the day
- Close with completion of the daily Exit Ticket (opportunity for informal assessment that guides effective preparation of subsequent lessons) as needed.

### Centers:

- I-Ready: <https://login.i-ready.com/> *i-Ready* makes the promise of differentiated instruction a practical reality for teachers and students. It was designed to get students excited about learning and to support teachers in the challenge of meeting the needs of all learners. Through the power of one intuitive system whose pieces were built from the ground up to work together, teachers have the tools they need to ensure students are on the road to proficiency.
- Zearn: <https://www.zearn.org/> *Zearn* Math is a K-5 math curriculum based on Eureka Math with top-rated materials for teacher-led and digital instruction.
- Teacher Toolbox; <https://teacher-toolbox.com/> A digital collection of K-8 resources to help you differentiate instruction to students performing on, below, and above grade level.

## NJSLA Assessment Evidence/Clarification Statements

NJSLA	Evidence Statement	Clarification	MP
4.NF.5	Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. For example, express $\frac{3}{10}$ as $\frac{30}{100}$ , and add $\frac{3}{10} + \frac{4}{100} = \frac{34}{100}$ .	<ul style="list-style-type: none"> <li>Tasks do not have a context.</li> </ul>	MP 7
4.NF.6	Use decimal notation for fractions with denominators 10 or 100. For example, rewrite 0.62 as $\frac{62}{100}$ ; describe a length as 0.62 meters; locate 0.62 on a number line diagram.	<ul style="list-style-type: none"> <li>Measuring to the nearest mm or cm is equivalent to measuring on the number line.</li> </ul>	MP 7
4.NF.7	Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols $>$ , $=$ , $<$ , or $\approx$ and justify the conclusions, e.g., by using a visual model.	<ul style="list-style-type: none"> <li>Tasks have “thin context” or no context.</li> <li>Justifying conclusions is not assessed here.</li> <li>Prompts do not provide visual fraction models; students may at their discretion draw visual fraction models as a strategy.</li> </ul>	MP 5,7
4.NF.Int.2	Solve one-step addition word problems. Content Scope: 4.NF.5, 4.NF.6	<ul style="list-style-type: none"> <li>Tasks are one of two kinds: Add To with result unknown, or Put Together with result unknown.</li> <li>See Table 2, p. 9 of the OA Progression document; these situations are sampled equally.</li> </ul>	MP 1
4.C.4-5	Base arithmetic explanations/reasoning on concrete referents such as diagrams (whether provided in the prompt or constructed by the student in her response), connecting the diagrams to a written (symbolic) method. Content Scope: Knowledge and skills articulated in 4.NF.C	<ul style="list-style-type: none"> <li>i) Tasks have “thin context” or no context.</li> <li>ii) Tasks are limited to denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100.</li> </ul>	MP 2,3,5,6

Student Name: \_\_\_\_\_ Task: \_\_\_\_\_ School: \_\_\_\_\_ Teacher: \_\_\_\_\_ Date: \_\_\_\_\_

"I CAN....."	STUDENT FRIENDLY RUBRIC				SCORE
	...a start 1	...getting there 2	...that's it 3	WOW! 4	
<b>Understand</b>	I need help.	I need some help.	I do not need help.	I can help a classmate.	
<b>Solve</b>	I am unable to use a strategy.	I can start to use a strategy.	I can solve it more than one way.	I can use more than one strategy and talk about how they get to the same answer.	
<b>Say or Write</b>	I am unable to say or write.	I can write or say some of what I did.	I can write and talk about what I did.  I can write or talk about why I did it.	I can write and say what I did and why I did it.	
<b>Draw or Show</b>	I am not able to draw or show my thinking.	I can draw, but not show my thinking; or I can show but not draw my thinking;	I can draw and show my thinking	I can draw, show and talk about my thinking.	



## Number Talks

### What does Number Talks look like?

- Students are near each other so they can communicate with each other (central meeting place)
- Students are mentally solving problems
- Students are given thinking time
- Thumbs up show when they are ready
- Teacher is recording students' thinking

### Communication

- Having to talk out loud about a problem helps students clarify their own thinking
- Allow students to listen to other's strategies and value other's thinking
- Gives the teacher the opportunity to hear student's thinking

### Mental Math

- When you are solving a problem mentally you must rely on what you know and understand about the numbers instead of memorized procedures
- You must be efficient when computing mentally because you can hold a lot of quantities in your head

### Thumbs Up

- This is just a signal to let you know that you have given your students enough time to think about the problem
- It will give you a picture of who is able to compute mentally and who is struggling
- It isn't as distracting as a waving hand

### Teacher as Recorder

- Allows you to record students' thinking in the correct notation
- Provides a visual to look at and refer back to
- Allows you to keep a record of the problems posed and which students offered specific strategies

### Purposeful Problems

- Start with small numbers so the students can learn to focus on the strategies instead of getting lost in the numbers
- Use a number string (a string of problems that are related to and scaffold each other)

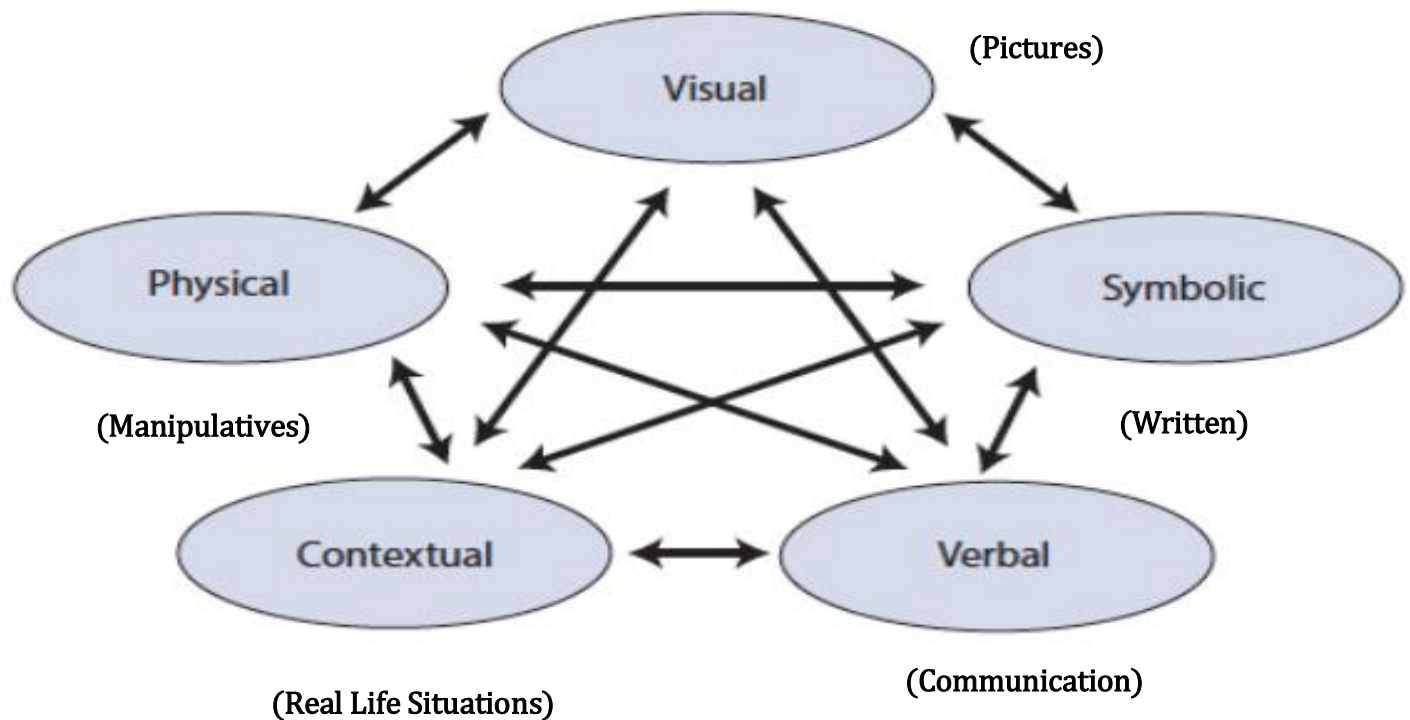
### Starting Number Talks in your Classroom

- Start with specific problems in mind
- Be prepared to offer a strategy from a previous student
- It is ok to put a student's strategy on the backburner
- Limit your number talks to about 15 minutes
- Ask a question, don't tell!

### The teacher asks questions:

- Who would like to share their thinking?
- Who did it another way?
- How many people solved it the same way as Billy?
- Does anyone have any questions for Billy?
- Billy, can you tell us where you got that 5?
- How did you figure that out?

## Use and Connection of Mathematical Representations



**The Lesh Translation Model**

Each oval in the model corresponds to one way to represent a mathematical idea.

**Visual:** When children draw pictures, the teacher can learn more about what they understand about a particular mathematical idea and can use the different pictures that children create to provoke a discussion about mathematical ideas. Constructing their own pictures can be a powerful learning experience for children because they must consider several aspects of mathematical ideas that are often assumed when pictures are pre-drawn for students.

**Physical:** The manipulatives representation refers to the unifix cubes, base-ten blocks, fraction circles, and the like, that a child might use to solve a problem. Because children can physically manipulate these objects, when used appropriately, they provide opportunities to compare relative sizes of objects, to identify patterns, as well as to put together representations of numbers in multiple ways.

**Verbal:** Traditionally, teachers often used the spoken language of mathematics but rarely gave students opportunities to grapple with it. Yet, when students do have opportunities to express their mathematical reasoning aloud, they may be able to make explicit some knowledge that was previously implicit for them.

**Symbolic:** Written symbols refer to both the mathematical symbols and the written words that are associated with them. For students, written symbols tend to be more abstract than the other representations. I tend to introduce symbols after students have had opportunities to make connections among the other representations, so that the students have multiple ways to connect the symbols to mathematical ideas, thus increasing the likelihood that the symbols will be comprehensible to students.

**Contextual:** A relevant situation can be any context that involves appropriate mathematical ideas and holds interest for children; it is often, but not necessarily, connected to a real-life situation.

### **The Lesh Translation Model: Importance of Connections**

As important as the ovals are in this model, another feature of the model is even more important than the representations themselves: The arrows! The arrows are important because they represent the connections students make between the representations. When students make these connections, they may be better able to access information about a mathematical idea, because they have multiple ways to represent it and, thus, many points of access.

Individuals enhance or modify their knowledge by building on what they already know, so the greater the number of representations with which students have opportunities to engage, the more likely the teacher is to tap into a student's prior knowledge. This "tapping in" can then be used to connect students' experiences to those representations that are more abstract in nature (such as written symbols). Not all students have the same set of prior experiences and knowledge. Teachers can introduce multiple representations in a meaningful way so that students' opportunities to grapple with mathematical ideas are greater than if their teachers used only one or two representations.

## Concrete Pictorial Abstract (CPA) Instructional Approach

The CPA approach suggests that there are three steps necessary for pupils to develop understanding of a mathematical concept.

**Concrete:** “Doing Stage”: Physical manipulation of objects to solve math problems.

**Pictorial:** “Seeing Stage”: Use of imaged to represent objects when solving math problems.

**Abstract:** “Symbolic Stage”: Use of only numbers and symbols to solve math problems.

CPA is a gradual systematic approach. Each stage builds on to the previous stage. Reinforcement of concepts are achieved by going back and forth between these representations and making connections between stages. Students will benefit from seeing parallel samples of each stage and how they transition from one to another.

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## Read, Draw, Write Process

**READ** the problem. Read it over and over.... And then read it again.

**DRAW** a picture that represents the information given. During this step students ask themselves: Can I draw something from this information? What can I draw? What is the best model to show the information? What conclusions can I make from the drawing?

**WRITE** your conclusions based on the drawings. This can be in the form of a number sentence, an equation, or a statement.

Students are able to draw a model of what they are reading to help them understand the problem. Drawing a model helps students see which operation or operations are needed, what patterns might arise, and which models work and do not work. Students must dive deeper into the problem by drawing models and determining which models are appropriate for the situation.

While students are employing the RDW process they are using several Standards for Mathematical Practice and in some cases, all of them.

## Mathematical Discourse and Strategic Questioning

Discourse involves asking strategic questions that elicit from students their understanding of the context and actions taking place in a problem, how a problem is solved and why a particular method was chosen. Students learn to critique their own and others' ideas and seek out efficient mathematical solutions.

While classroom discussions are nothing new, the theory behind classroom discourse stems from constructivist views of learning where knowledge is created internally through interaction with the environment. It also fits in with socio-cultural views on learning where students working together are able to reach new understandings that could not be achieved if they were working alone.

Underlying the use of discourse in the mathematics classroom is the idea that mathematics is primarily about reasoning not memorization. Mathematics is not about remembering and applying a set of procedures but about developing understanding and explaining the processes used to arrive at solutions.

### Teacher Questioning:

Asking better questions can open new doors for students, promoting mathematical thinking and classroom discourse. Can the questions you're asking in the mathematics classroom be answered with a simple "yes" or "no," or do they invite students to deepen their understanding?



The most  
important thing  
is to **NEVER**  
stop  
questioning

*Albert Einstein*

To help you encourage deeper discussions, here are 100 questions to incorporate into your instruction by Gladis Kersaint, mathematics expert and advisor for Ready Mathematics.

Dr.

**100** questions that promote  
**Mathematical Discourse**

Help students **work together** to make sense of mathematics

- 1 What **strategy** did you use?
- 2 Do you **agree**?
- 3 Do you **disagree**?
- 4 Would you **ask the rest of the class** that question?
- 5 Could you **share your method** with the class?
- 6 What part of what he said **do you understand**?
- 7 Would someone like to **share** \_\_\_?
- 8 Can you **convince the rest of us** that your answer makes sense?
- 9 **What do others think** about what [student] said?
- 10 Can someone **retell or restate** [student]'s explanation?
- 11 Did you **work together**? In what way?
- 12 Would anyone like to **add to what was said**?
- 13 Have you **discussed** this with your group? With others?
- 14 Did anyone get a **different answer**?
- 15 **Where** would you go for **help**?
- 16 **Did everybody get a fair chance** to talk, use the manipulatives, or be the recorder?
- 17 How could you help another student **without telling them the answer**?
- 18 **How would you explain** \_\_\_ to someone who missed class today?

Help students **rely more on themselves** to determine whether something is **mathematically correct**

- 19 Is this a **reasonable answer**?
- 20 Does that make **sense**?
- 21 **Why** do you think that? Why is that true?
- 22 Can you **draw a picture or make a model** to show that?
- 23 **How** did you reach that conclusion?
- 24 Does anyone want to **revise** his or her answer?
- 25 **How were you sure** your answer was right?

Ready

## Help students learn to reason mathematically

- 26 How did you **begin** to think about this problem?
- 27 What is **another way** you could solve this problem?
- 28 How could you **prove** \_\_\_\_\_?
- 29 Can you **explain how your answer is different from or the same as** [student]'s answer?
- 30 Let's **break the problem into parts**. What would the parts be?
- 31 Can you **explain this part more specifically**?
- 32 Does that **always work**?
- 33 Can you think of a case where that **wouldn't work**?
- 34 How did you **organize** your information? Your thinking?

## Help students with problem comprehension

- 39 What is this problem about? What can you **tell me about it**?
- 40 Do you need to **define or set limits** for the problem?
- 41 How would you **interpret** that?
- 42 Could you **reword that in simpler terms**?
- 43 Is there something that can be **eliminated** or that is **missing**?
- 44 Could you **explain** what the problem is asking?
- 45 What **assumptions** do you have to make?
- 46 What do you **know** about this part?
- 47 Which words were **most important**? Why?

## Help students evaluate their own processes and engage in productive peer interaction

- 35 What do you need to do **next**?
- 36 What have you **accomplished**?
- 37 What are your **strengths and weaknesses**?
- 38 Was your **group participation appropriate and helpful**?



## Help students learn to **conjecture, invent, and solve problems**

- 48 What would happen if \_\_\_?
- 49 Do you see a **pattern**?
- 50 What are some **possibilities** here?
- 51 Where could you find the **information** you need?
- 52 How would you **check your steps** or your answer?
- 53 What **did not work**?
- 54 How is your solution method the **same as or different from** [student]'s method?
- 55 Other than retracing your steps, **how can you determine** if your answers are appropriate?
- 56 How did you **organize** the information? Do you have a **record**?
- 57 How could you solve this using **tables, lists, pictures, diagrams**, etc.?
- 58 What have you tried? What **steps** did you take?
- 59 How would it look if you used this **model** or these **materials**?
- 60 How would you draw a **diagram or make a sketch** to solve the problem?
- 61 Is there **another possible answer**? If so, explain.
- 62 Is there **another way to solve** the problem?
- 63 Is there **another model** you could use to solve the problem?
- 64 Is there anything you've **overlooked**?
- 65 **How did you think** about the problem?
- 66 What was your **estimate or prediction**?
- 67 How **confident** are you in your answer?
- 68 **What else** would you like to know?
- 69 What do you think comes **next**?
- 70 Is the solution **reasonable**, considering the context?
- 71 Did you have a **system**? Explain it.
- 72 Did you have a **strategy**? Explain it.
- 73 Did you have a **design**? Explain it.





## Help students learn to connect mathematics, its ideas, and its application

- 74 What is the **relationship** between \_\_\_ and \_\_\_?
- 75 Have we ever solved a problem **like this before**?
- 76 What uses of mathematics did you find in the **newspaper** last night?
- 77 What is the **same**?
- 78 What is **different**?
- 79 Did you use skills or build on concepts that were **not necessarily mathematical**?
- 80 Which **skills or concepts** did you use?
- 81 What **ideas** have we explored before that were useful in solving this problem?

- 82 Is there a **pattern**?
- 83 **Where else** would this strategy be useful?
- 84 How does this **relate** to \_\_\_?
- 85 Is there a **general rule**?
- 86 Is there a **real-life situation** where this could be used?
- 87 How would your method work with **other problems**?
- 88 What other problem does this seem to **lead to**?

### Help students persevere

- 95 What was **one thing you learned** (or two, or more)?
- 96 Did you **notice any patterns**? If so, describe them.
- 97 What **mathematics topics** were used in this investigation?
- 98 What were the **mathematical ideas** in this problem?
- 99 What is mathematically **different about these two situations**?
- 100 What are the **variables** in this problem? What stays **constant**?

- 89 Have you tried making a **guess**?
- 90 **What else** have you tried?
- 91 Would **another method** work as well or better?
- 92 Is there **another way** to draw, explain, or say that?
- 93 Give me another **related problem**. Is there an easier problem?
- 94 How would you **explain** what you know right now?

### Help students focus on the mathematics from activities

## Conceptual Understanding

Students demonstrate conceptual understanding in mathematics when they provide evidence that they can:

- recognize, label, and generate examples of concepts;
- use and interrelate models, diagrams, manipulatives, and varied representations of concepts;
- identify and apply principles; know and apply facts and definitions;
- compare, contrast, and integrate related concepts and principles; and
- recognize, interpret, and apply the signs, symbols, and terms used to represent concepts.

Conceptual understanding reflects a student's ability to reason in settings involving the careful application of concept definitions, relations, or representations of either.

## Procedural Fluency

Procedural fluency is the ability to:

- apply procedures accurately, efficiently, and flexibly;
- to transfer procedures to different problems and contexts;
- to build or modify procedures from other procedures; and
- to recognize when one strategy or procedure is more appropriate to apply than another.

Procedural fluency is more than memorizing facts or procedures, and it is more than understanding and being able to use one procedure for a given situation. Procedural fluency builds on a foundation of conceptual understanding, strategic reasoning, and problem solving (NGA Center & CCSSO, 2010; NCTM, 2000, 2014). Research suggests that once students have memorized and practiced procedures that they do not understand, they have less motivation to understand their meaning or the reasoning behind them (Hiebert, 1999). Therefore, the development of students' conceptual understanding of procedures should precede and coincide with instruction on procedures.

## Math Fact Fluency: Automaticity

Students who possess math fact fluency can recall math facts with automaticity. Automaticity is the ability to do things without occupying the mind with the low-level details required, allowing it to become an automatic response pattern or habit. It is usually the result of learning, repetition, and practice.

### 3-5 Math Fact Fluency Expectation

**3.OA.C.7:** Single-digit products and quotients (Products from memory by end of Grade 3)

**3.NBT.A.2:** Add/subtract within 1000

**4.NBT.B.4:** Add/subtract within 1,000,000/ Use of Standard Algorithm

**5.NBT.B.5:** Multi-digit multiplication/ Use of Standard Algorithm

## Evidence of Student Thinking

Effective classroom instruction and more importantly, improving student performance, can be accomplished when educators know how to elicit evidence of students' understanding on a daily basis. Informal and formal methods of collecting evidence of student understanding enable educators to make positive instructional changes. An educators' ability to understand the processes that students use helps them to adapt instruction allowing for student exposure to a multitude of instructional approaches, resulting in higher achievement. By highlighting student thinking and misconceptions, and eliciting information from more students, all teachers can collect more representative evidence and can therefore better plan instruction based on the current understanding of the entire class.

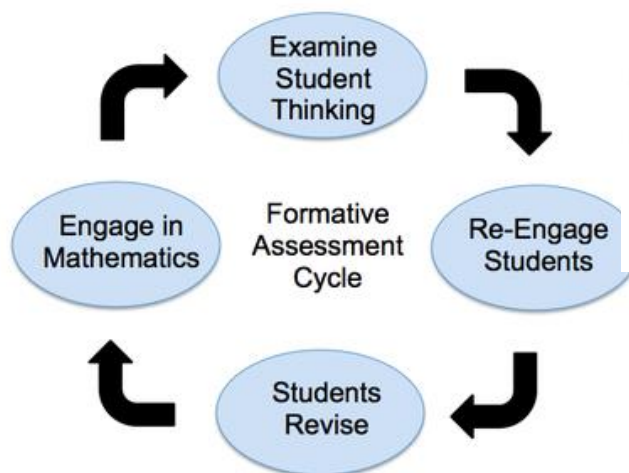
## Mathematical Proficiency

To be mathematically proficient, a student must have:

- Conceptual understanding: comprehension of mathematical concepts, operations, and relations;
- Procedural fluency: skill in carrying out procedures flexibly, accurately, efficiently, and appropriately;
- Strategic competence: ability to formulate, represent, and solve mathematical problems;
- Adaptive reasoning: capacity for logical thought, reflection, explanation, and justification;
- Productive disposition: habitual inclination to see mathematics as sensible, useful, and worthwhile, coupled with a belief in diligence and one's own efficacy.

## Evidence should:

- Provide a window in student thinking;
- Help teachers to determine the extent to which students are reaching the math learning goals; and
- Be used to make instructional decisions during the lesson and to prepare for subsequent lessons.



*Formative assessment is an essentially interactive process, in which the teacher can find out whether what has been taught has been learned, and if not, to do something about it. Day-to-day formative assessment is one of the most powerful ways of improving learning in the mathematics classroom.*

(William 2007, pp. 1054; 1091)

## Connections to the Mathematical Practices

### Student Friendly Connections to the Mathematical Practices

1. I can solve problems without giving up.
2. I can think about numbers in many ways.
3. I can explain my thinking and try to understand others.
4. I can show my work in many ways.
5. I can use math tools and tell why I choose them.
6. I can work carefully and check my work.
7. I can use what I know to solve new problems.
8. I can discover and use short cuts.

### The Standards for Mathematical Practice:

Describe varieties of expertise that mathematics educators at all levels should seek to develop in their students.

<b>1</b>	<p><b>Make sense of problems and persevere in solving them</b></p> <p>Mathematically proficient students in grade 4 know that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. Fourth graders may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, “Does this make sense?” They listen to the strategies of others and will try different approaches. They often will use another method to check their answers.</p>
<b>2</b>	<p><b>Reason abstractly and quantitatively</b></p> <p>Mathematically proficient fourth graders should recognize that a number represents a specific quantity. They connect the quantity to written symbols and create a logical representation of the problem at hand, considering both the appropriate units involved and the meaning of quantities. They extend this understanding from whole numbers to their work with fractions and decimals. Students write simple expressions, record calculations with numbers, and represent or round numbers using place value concepts.</p>
<b>3</b>	<p><b>Construct viable arguments and critique the reasoning of others</b></p> <p>In fourth grade mathematically proficient students may construct arguments using concrete referents, such as objects, pictures, and drawings. They explain their thinking and make connections between models and equations. They refine their mathematical communication skills as they participate in mathematical discussions involving questions like “How did you get that?” and “Why is that true?” They explain their thinking to others and respond to others’ thinking.</p>
<b>4</b>	<p><b>Model with mathematics</b></p> <p>Mathematically proficient fourth grade students experiment with representing problem situations in multiple ways including numbers, words (mathematical language), drawing pictures, using objects, making a chart, list, or graph, creating equations, etc. Students need opportunities to connect the different representations and explain the connections. They should be able to use all of these representations as needed. Fourth graders should evaluate their results in the context of the situation and reflect on whether the results make sense.</p>

5	<b>Use appropriate tools strategically</b>
	Mathematically proficient fourth graders consider the available tools(including estimation) when solving a mathematical problem and decide when certain tools might be helpful. For instance, they may use graph paper or a number line to represent and compare decimals and protractors to measure angles. They use other measurement tools to understand the relative size of units within a system and express measurements given in larger units in terms of smaller units.
6	<b>Attend to precision</b>
	As fourth graders develop their mathematical communication skills, they try to use clear and precise language in their discussions with others and in their own reasoning. They are careful about specifying units of measure and state the meaning of the symbols they choose. For instance, they use appropriate labels when creating a line plot.
7	<b>Look for and make use of structure</b>
	In fourth grade mathematically proficient students look closely to discover a pattern or structure. For instance, students use properties of operations to explain calculations (partial products model). They relate representations of counting problems such as tree diagrams and arrays to the multiplication principal of counting. They generate number or shape patterns that follow a given rule.
8	<b>Look for and express regularity in repeated reasoning</b>
	Students in fourth grade should notice repetitive actions in computation to make generalizations Students use models to explain calculations and understand how algorithms work. They also use models to examine patterns and generate their own algorithms. For example, students use visual fraction models to write equivalent fractions.

## Effective Mathematics Teaching Practices

**Establish mathematics goals to focus learning.** Effective teaching of mathematics establishes clear goals for the mathematics that students are learning, situates goals within learning progressions, and uses the goals to guide instructional decisions.

**Implement tasks that promote reasoning and problem solving.** Effective teaching of mathematics engages students in solving and discussing tasks that promote mathematical reasoning and problem solving and allow multiple entry points and varied solution strategies.

**Use and connect mathematical representations.** Effective teaching of mathematics engages students in making connections among mathematical representations to deepen understanding of mathematics concepts and procedures and as tools for problem solving.

**Facilitate meaningful mathematical discourse.** Effective teaching of mathematics facilitates discourse among students to build shared understanding of mathematical ideas by analyzing and comparing student approaches and arguments.

**Pose purposeful questions.** Effective teaching of mathematics uses purposeful questions to assess and advance students' reasoning and sense making about important mathematical ideas and relationships.

**Build procedural fluency from conceptual understanding.** Effective teaching of mathematics builds fluency with procedures on a foundation of conceptual understanding so that students, over time, become skillful in using procedures flexibly as they solve contextual and mathematical problems.

**Support productive struggle in learning mathematics.** Effective teaching of mathematics consistently provides students, individually and collectively, with opportunities and supports to engage in productive struggle as they grapple with mathematical ideas and relationships.

**Elicit and use evidence of student thinking.** Effective teaching of mathematics uses evidence of student thinking to assess progress toward mathematical understanding and to adjust instruction continually in ways that support and extend learning.

<b><u>5 Practices for Orchestrating Productive Mathematics Discussions</u></b>	
Practice	Description/ Questions
1. Anticipating	<p>What strategies are students likely to use to approach or solve a challenging high-level mathematical task?</p> <p>How do you respond to the work that students are likely to produce?</p> <p>Which strategies from student work will be most useful in addressing the mathematical goals?</p>
2. Monitoring	<p>Paying attention to what and how students are thinking during the lesson.</p> <p>Students working in pairs or groups</p> <p>Listening to and making note of what students are discussing and the strategies they are using</p> <p>Asking students questions that will help them stay on track or help them think more deeply about the task. (Promote productive struggle)</p>
3. Selecting	<p>This is the process of deciding the <i>what</i> and the <i>who</i> to focus on during the discussion.</p>
4. Sequencing	<p>What order will the solutions be shared with the class?</p>
5. Connecting	<p>Asking the questions that will make the mathematics explicit and understandable.</p> <p>Focus must be on mathematical meaning and relationships; making links between mathematical ideas and representations.</p>

## MATH CENTERS/ WORKSTATIONS

*Math workstations* allow students to engage in authentic and meaningful hands-on learning. They often last for several weeks, giving students time to reinforce or extend their prior instruction. Before students have an opportunity to use the materials in a station, introduce them to the whole class, several times. Once they have an understanding of the concept, the materials are then added to the work stations.

### Station Organization and Management Sample

Teacher A has 12 containers labeled 1 to 12. The numbers correspond to the numbers on the rotation chart. She pairs students who can work well together, who have similar skills, and who need more practice on the same concepts or skills. Each day during math work stations, students use the center chart to see which box they will be using and who their partner will be. Everything they need for their station will be in their box. **Each station is differentiated.** If students need more practice and experience working on numbers 0 to 10, those will be the only numbers in their box. If they are ready to move on into the teens, then she will place higher number activities into the box for them to work with.



In the beginning there is a lot of prepping involved in gathering, creating, and organizing the work stations. However, once all of the initial work is complete, the stations are easy to manage. Many of her stations stay in rotation for three or four weeks to give students ample opportunity to master the skills and concepts.

Read *Math Work Stations* by Debbie Diller.

In her book, she leads you step-by-step through the process of implementing work stations.



**MATH WORKSTATION INFORMATION CARD**

**Math Workstation:** \_\_\_\_\_

**Time:**

**NJSLS:**

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**Objective(s):** By the end of this task, I will be able to:

- \_\_\_\_\_
- \_\_\_\_\_
- \_\_\_\_\_

**Task(s):**

- \_\_\_\_\_
- \_\_\_\_\_
- \_\_\_\_\_
- \_\_\_\_\_

**Exit Ticket:**

- \_\_\_\_\_
- \_\_\_\_\_
- \_\_\_\_\_

**MATH WORKSTATION SCHEDULE**

**Week of:** \_\_\_\_\_

DAY	Technology Lab	Problem Solving Lab	Fluency Lab	Math Journal	Small Group Instruction
Mon.	Group ____	Group ____	Group ____	Group ____	BASED ON CURRENT OB- SERVATIONAL DA- TA
Tues.	Group ____	Group ____	Group ____	Group ____	
Wed.	Group ____	Group ____	Group ____	Group ____	
Thurs.	Group ____	Group ____	Group ____	Group ____	
Fri.	Group ____	Group ____	Group ____	Group ____	

**INSTRUCTIONAL GROUPING**

	GROUP A		GROUP B
1		1	
2		2	
3		3	
4		4	
5		5	
6		6	
	GROUP C		GROUP D
1		1	
2		2	
3		3	
4		4	
5		5	

Fourth Grade PLD Rubric

Got It		Not There Yet		
Evidence shows that the student essentially has the target concept or big math idea.		Student shows evidence of a major misunderstanding, incorrect concepts or procedure, or a failure to engage in the task.		
PLD Level 5: 100% Distinguished command	PLD Level 4: 89% Strong Command	PLD Level 3: 79% Moderate Command	PLD Level 2: 69% Partial Command	PLD Level 1: 59% Little Command
<p>Student work shows <b>distinct levels of understanding</b> of the mathematics.</p> <p>Student <b>constructs and communicates a complete response</b> based on explanations/reasoning using the:</p> <ul style="list-style-type: none"> <li>• Tools:                             <ul style="list-style-type: none"> <li>○ Manipulatives</li> <li>○ Five Frame</li> <li>○ Ten Frame</li> <li>○ Number Line</li> <li>○ Part-Part-Whole Model</li> </ul> </li> <li>• Strategies:                             <ul style="list-style-type: none"> <li>○ Drawings</li> <li>○ Counting All</li> <li>○ Count On/Back</li> <li>○ Skip Counting</li> <li>○ Making Ten</li> <li>○ Decomposing Number</li> </ul> </li> <li>• Precise use of math vocabulary</li> </ul> <p>Response includes an <b>efficient and logical progression</b> of mathematical reasoning and understanding.</p>	<p>Student work shows <b>strong levels of understanding</b> of the mathematics.</p> <p>Student <b>constructs and communicates a complete response</b> based on explanations/reasoning using the:</p> <ul style="list-style-type: none"> <li>• Tools:                             <ul style="list-style-type: none"> <li>○ Manipulatives</li> <li>○ Five Frame</li> <li>○ Ten Frame</li> <li>○ Number Line</li> <li>○ Part-Part-Whole Model</li> </ul> </li> <li>• Strategies:                             <ul style="list-style-type: none"> <li>○ Drawings</li> <li>○ Counting All</li> <li>○ Count On/Back</li> <li>○ Skip Counting</li> <li>○ Making Ten</li> <li>○ Decomposing Number</li> </ul> </li> <li>• Precise use of math vocabulary</li> </ul> <p>Response includes a <b>logical progression</b> of mathematical reasoning and understanding.</p>	<p>Student work shows <b>moderate levels of understanding</b> of the mathematics.</p> <p>Student <b>constructs and communicates a complete response</b> based on explanations/reasoning using the:</p> <ul style="list-style-type: none"> <li>• Tools:                             <ul style="list-style-type: none"> <li>○ Manipulatives</li> <li>○ Five Frame</li> <li>○ Ten Frame</li> <li>○ Number Line</li> <li>○ Part-Part-Whole Model</li> </ul> </li> <li>• Strategies:                             <ul style="list-style-type: none"> <li>○ Drawings</li> <li>○ Counting All</li> <li>○ Count On/Back</li> <li>○ Skip Counting</li> <li>○ Making Ten</li> <li>○ Decomposing Number</li> </ul> </li> <li>• Precise use of math vocabulary</li> </ul> <p>Response includes a <b>logical but incomplete progression</b> of mathematical reasoning and understanding. Contains <b>minor errors</b>.</p>	<p>Student work shows <b>partial understanding</b> of the mathematics.</p> <p>Student <b>constructs and communicates an incomplete response</b> based on student's attempts of explanations/reasoning using the:</p> <ul style="list-style-type: none"> <li>• Tools:                             <ul style="list-style-type: none"> <li>○ Manipulatives</li> <li>○ Five Frame</li> <li>○ Ten Frame</li> <li>○ Number Line</li> <li>○ Part-Part-Whole Model</li> </ul> </li> <li>• Strategies:                             <ul style="list-style-type: none"> <li>○ Drawings</li> <li>○ Counting All</li> <li>○ Count On/Back</li> <li>○ Skip Counting</li> <li>○ Making Ten</li> <li>○ Decomposing Number</li> </ul> </li> <li>• Precise use of math vocabulary</li> </ul> <p>Response includes an <b>incomplete or illogical progression</b> of mathematical reasoning and understanding.</p>	<p>Student work shows <b>little understanding</b> of the mathematics.</p> <p>Student <b>attempts to construct and communicates</b> a response using the:</p> <ul style="list-style-type: none"> <li>• Tools:                             <ul style="list-style-type: none"> <li>○ Manipulatives</li> <li>○ Five Frame</li> <li>○ Ten Frame</li> <li>○ Number Line</li> <li>○ Part-Part-Whole Model</li> </ul> </li> <li>• Strategies:                             <ul style="list-style-type: none"> <li>○ Drawings</li> <li>○ Counting All</li> <li>○ Count On/Back</li> <li>○ Skip Counting</li> <li>○ Making Ten</li> <li>○ Decomposing Number</li> </ul> </li> <li>• Precise use of math vocabulary</li> </ul> <p>Response includes <b>limited evidence of the progression</b> of mathematical reasoning and understanding.</p>
<b>5 points</b>	<b>4 points</b>	<b>3 points</b>	<b>2 points</b>	<b>1 point</b>

## DATA DRIVEN INSTRUCTION

Formative assessments inform instructional decisions. Taking inventories and assessments, observing reading and writing behaviors, studying work samples and listening to student talk are essential components of gathering data. When we take notes, ask questions in a student conference, lean in while a student is working or utilize a more formal assessment we are gathering data. Learning how to take the data and record it in a meaningful way is the beginning of the cycle.

Analysis of the data is an important step in the process. What is this data telling us? We must look for patterns, as well as compare the notes we have taken with work samples and other assessments. We need to decide what are the strengths and needs of individuals, small groups of students and the entire class. Sometimes it helps to work with others at your grade level to analyze the data.

Once we have analyzed our data and created our findings, it is time to make informed instructional decisions. These decisions are guided by the following questions:

- What mathematical practice(s) and strategies will I utilize to teach to these needs?
- What sort of grouping will allow for the best opportunity for the students to learn what it is I see as a need?
- Will I teach these strategies to the whole class, in a small guided group or in an individual conference?
- Which method and grouping will be the most effective and efficient? What specific objective(s) will I be teaching?

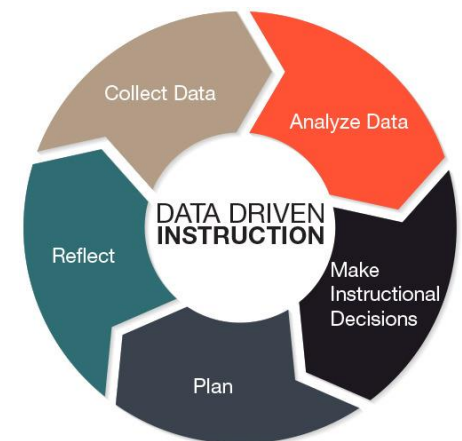
Answering these questions will help inform instructional decisions and will influence lesson planning.

Then we create our instructional plan for the unit/month/week/day and specific lessons.

It's important now to reflect on what you have taught.

Did you observe evidence of student learning through your checks for understanding, and through direct application in student work?

What did you hear and see students doing in their reading and writing?



**Data Analysis Form**

**School:** \_\_\_\_\_ **Teacher:** \_\_\_\_\_ **Date:** \_\_\_\_\_

**Assessment:** \_\_\_\_\_ **NJSLS:** \_\_\_\_\_

GROUPS (STUDENT INITIALS)	SUPPORT PLAN	PROGRESS
MASTERED (86% - 100%) (PLD 4/5):		
DEVELOPING (67% - 85%) (PLD 3):		
INSECURE (51%-65%) (PLD 2):		
BEGINNING (0%-50%) (PLD 1):		

### **MATH PORTFOLIO EXPECTATIONS**

**The Student Assessment Portfolios for Mathematics** are used as a means of documenting and evaluating students' academic growth and development over time and in relation to the NJSL. The September task entry(-ies) should reflect the prior year content and *can serve* as an additional baseline measure.

All tasks contained within the **Student Assessment Portfolios** should be aligned to NJSL and be “practice forward” (closely aligned to the Standards for Mathematical Practice).

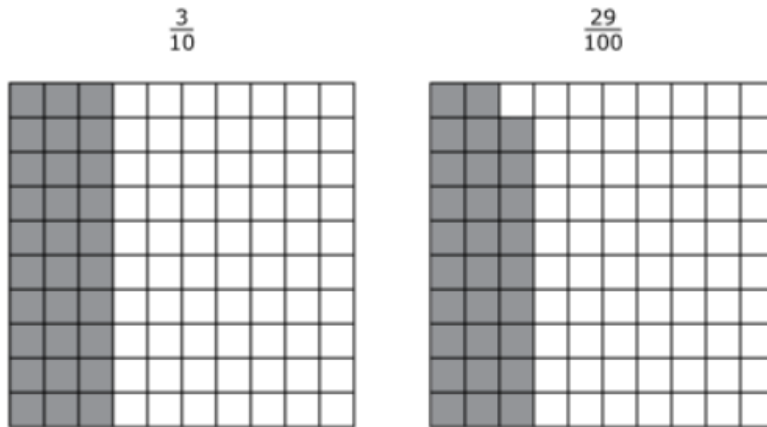
Four (4) or more additional tasks will be included in the **Student Assessment Portfolios** for Student Reflection and will be labeled as such.

### **GENERAL PORTFOLIO EXPECTATIONS:**

- Tasks contained within the Student Assessment Portfolios are “practice forward” and denoted as “Individual”, “Partner/Group”, and “Individual w/Opportunity for Student Interviews<sup>1</sup>”.
- Each Student Assessment Portfolio should contain a “Task Log” that documents all tasks, standards, and rubric scores aligned to the performance level descriptors (PLDs).
- Student work should be attached to a completed rubric; with appropriate teacher feedback on student work.
- Students will have multiple opportunities to revisit certain standards. Teachers will capture each additional opportunity “as a new and separate score” in the task log.
- A 2-pocket folder for each Student Assessment Portfolio is *recommended*.
- All Student Assessment Portfolio entries should be scored and recorded as an Authentic Assessment grade (25%)<sup>2</sup>.
- All Student Assessment Portfolios must be clearly labeled, maintained for all students, inclusive of constructive teacher and student feedback and accessible for review.

**4<sup>TH</sup> Grade Authentic Assessment: Jessica's Grids**

Jessica shades two grids that each equal one whole to represent and compare the fractions  $\frac{3}{10}$  and  $\frac{29}{100}$ .



Part A

Write the decimal that represents  $\frac{3}{10}$  and the decimal that represents  $\frac{29}{100}$  in each box to create a true comparison.

<

Part B

Jessica says that  $\frac{3}{10} + \frac{29}{100} = \frac{32}{100}$  because  $3 + 29 = 32$  and there are 100 squares in each of the grids. Explain how you know Jessica is incorrect by using the grids or the decimal inequality you created. Then find the correct sum. Show your work or explain.

Fourth Grade Unit 4: Decimal Fraction

CCSS.MATH.CONTENT.4.NF.C.5

Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100.<sup>2</sup> For example, express  $\frac{3}{10}$  as  $\frac{30}{100}$ , and add  $\frac{3}{10} + \frac{4}{100} = \frac{34}{100}$ .

CCSS.MATH.CONTENT.4.NF.C.6

Use decimal notation for fractions with denominators 10 or 100. For example, rewrite  $\frac{62}{100}$  as 0.62; describe a length as 0.62 meters; locate 0.62 on a number line diagram.

**Part A**

Score	Description
1	<p>Student response includes the following element:</p> <ul style="list-style-type: none"> <li><b>Computation component: 1 point</b></li> </ul> <p><math>0.29 &lt; 0.3</math></p>
0	Student response is incorrect or irrelevant

**Part B**

Score	Description
3	<p>Student response includes the following 3 elements</p> <ul style="list-style-type: none"> <li><b>Reasoning component: 2 points</b> <ol style="list-style-type: none"> <li>Valid explanation, using the grids or the decimal inequality created in Part A, of why Jessica is incorrect. Note: An explanation on how <math>\frac{3}{10}</math> is equivalent to <math>\frac{30}{100}</math> or 0.3 must be provided. If using <math>\frac{3}{10}</math> equivalent to <math>\frac{30}{100}</math>, the explanation must be based off the grids. Simply stating <math>\frac{3}{10}</math> is equivalent to <math>\frac{30}{100}</math> is not sufficient for credit. A response using the decimal comparison model, <math>\frac{3}{10}</math> equivalent to 0.3, is also acceptable.</li> <li>Valid work or explanation of how to find the correct sum</li> </ol> </li> <li><b>Computation component: 1 point</b> <ol style="list-style-type: none"> <li>Correct sum, <math>\frac{59}{100}</math> (or equivalent)</li> </ol> </li> </ul> <p><u>Sample Student Response:</u>            Jessica tried to add tenths and hundredths. She used the ten columns on the <math>\frac{3}{10}</math> grid and didn't count the squares because then she would have used <math>\frac{30}{100}</math>.            On the grid, <math>\frac{3}{10}</math> is the same as <math>\frac{30}{100}</math> because 3 rows of 10 on the grid is equal to 0.3 or 0.30, which is <math>\frac{30}{100}</math>.            When you add the 30 squares covered by <math>\frac{3}{10}</math> to the 29 squares covered by <math>\frac{29}{100}</math>, you get 59 squares out of 100, or <math>\frac{59}{100}</math>.</p>



Fourth Grade Unit 4: Decimal Fraction

	<p>Note:</p> <ul style="list-style-type: none"> <li>- Students may alternatively use the decimal comparison model to explain that <math>\frac{3}{10}</math> is equal to 0.3 or 0.30, which is 30 hundredths.</li> <li>- Students may alternatively use the decimal comparison model to explain that when you add 0.30 and 0.29 you get 0.59, which is <math>\frac{59}{100}</math>.</li> </ul>
2	Student response includes 2 of the 3 elements.
1	Student response includes 1 of the 3 elements.
0	Student response is incorrect or irrelevant.

Level 5: Distinguished Command	Level 4: Strong Command	Level 3: Moderate Command	Level 2: Partial Command	Level 1: No Command
<p>Student correctly answers and clearly constructs and communicates a complete response based on explanations/reasoning using :</p> <ul style="list-style-type: none"> <li>• Concepts of place value and division</li> <li>• Strategies based on place value and the properties of operations</li> </ul> <p>Response includes an <b>efficient</b> and logical progression of steps.</p>	<p>Student correctly answers and clearly constructs and communicates a complete response with one minor calculation error based on explanations/reasoning using:</p> <ul style="list-style-type: none"> <li>• Concepts of place value and division</li> <li>• Strategies based on place value and the properties of operations.</li> </ul> <p>Response includes a <b>logical</b> progression of steps</p>	<p>Student answers, clearly constructs, and communicates a complete response with minor calculation errors based on explanations/reasoning using:</p> <ul style="list-style-type: none"> <li>• Concepts of place value and division</li> <li>• Strategies based on place value and the properties of operations</li> </ul> <p>Response includes a <b>logical but incomplete</b> progression of steps. Minor calculation errors.</p>	<p>Student answers, clearly constructs, and communicates a complete response with major calculation errors and/or conceptual errors based on explanations/reasoning using:</p> <ul style="list-style-type: none"> <li>• Concepts of place value and division</li> <li>• Strategies based on place value and the properties of operations</li> </ul> <p>Response includes an <b>incomplete or illogical</b> progression of steps.</p>	<p>The student shows no work or justification.</p>

## Core Instructional and Supplemental Materials (K-5)

EUREKA MATH V. 2019  
(GREAT MINDS)

GRADE	TEACHER RESOURCES	STUDENT RESOURCES
<b>K</b> (v. 2019.)	<ul style="list-style-type: none"> <li>• <a href="#">Teacher Edition: Module 1-6</a></li> <li>• Eureka Math Teacher Resource Pack</li> <li>• Eureka K-5 PD Toolkit</li> </ul>	<ul style="list-style-type: none"> <li>• Learn Workbook Set: Module 1-6</li> <li>• Succeed Workbook Set: Module 1-6</li> <li>• Practice Workbook, Fluency: Module 1-6</li> </ul>
<b>1</b>	<ul style="list-style-type: none"> <li>• <a href="#">Teacher Edition: Module 1-6</a></li> <li>• Eureka Math Teacher Resource Pack</li> <li>• Eureka K-5 PD Toolkit</li> </ul>	<ul style="list-style-type: none"> <li>• Learn Workbook Set: Module 1-6</li> <li>• Succeed Workbook Set: Module 1-6</li> <li>• Practice Workbook, Fluency: Module 1-6</li> </ul>
<b>2</b>	<ul style="list-style-type: none"> <li>• <a href="#">Teacher Edition: Module 1-8</a></li> <li>• Eureka Math Teacher Resource Pack</li> <li>• Eureka K-5 PD Toolkit</li> </ul>	<ul style="list-style-type: none"> <li>• Learn Workbook Set: Module 1-8</li> <li>• Succeed Workbook Set: Module 1-8</li> <li>• Practice Workbook, Fluency: Module 1-8</li> </ul>
<b>3</b>		
<b>4</b>	<ul style="list-style-type: none"> <li>• <a href="#">Teacher Edition: Module 1-7</a></li> <li>• Eureka Math Teacher Resource Pack</li> <li>• Eureka K-5 PD Toolkit</li> </ul>	<ul style="list-style-type: none"> <li>• Learn Workbook Set: Module 1-7</li> <li>• Succeed Workbook Set: Module 1-7</li> <li>• Practice Workbook, Fluency: Module 1-7</li> </ul>
<b>5</b>	<ul style="list-style-type: none"> <li>• <a href="#">Teacher Edition: Module 1-7</a></li> <li>• Eureka Math Teacher Resource Pack</li> <li>• Eureka K-5 PD Toolkit</li> </ul>	<ul style="list-style-type: none"> <li>• Learn Workbook Set: Module 1-7</li> <li>• Succeed Workbook Set: Module 1-7</li> <li>• Practice Workbook, Fluency: Module 1-7</li> </ul>
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**MATH IN FOCUS v. 2015**  
(HOUGHTON MIFFLIN HARCOURT)

GRADE	TEACHER RESOURCES	STUDENT RESOURCES
<b>K</b>	<ul style="list-style-type: none"> <li>• <b>Teacher Edition (A &amp; B)</b></li> <li>• Implementation Guide</li> <li>• Assessment Package</li> <li>• Enrichment Bundle</li> <li>• Extra Practice Set</li> <li>• Teacher and Student Activity Cards</li> <li>• Home -to- School Connection Book</li> <li>• Online Teacher Technology Kit</li> <li>• Big Book Set</li> <li>• Online Interactive Whiteboard Lessons</li> </ul>	<ul style="list-style-type: none"> <li>• Student Edition A – Pt. 1</li> <li>• Student Edition A – Pt. 2</li> <li>• Student Edition B – Pt. 1</li> <li>• Student Edition B – Pt. 2</li> <li>• Online Student Technology Kit</li> </ul>
<b>1</b>	<ul style="list-style-type: none"> <li>• <b>Teacher Edition (A &amp; B)</b></li> <li>• Implementation Guide</li> <li>• Assessment Package</li> <li>• Enrichment Bundle</li> <li>• Extra Practice Guide</li> <li>• Reteaching Guide</li> <li>• Home -to- School Connection Book</li> <li>• Online Teacher Technology Kit</li> <li>• Fact Fluency</li> <li>• Online Interactive Whiteboard Lessons</li> </ul>	<ul style="list-style-type: none"> <li>• Student Texts (A &amp; B)</li> <li>• Student Workbooks</li> <li>• Online Student Technology Kit</li> <li>• Student Interactivities</li> </ul>
<b>2-5</b>	<ul style="list-style-type: none"> <li>• <b>Teacher Edition (A &amp; B)</b></li> <li>• Implementation Guide</li> <li>• Assessment Package</li> <li>• Enrichment Bundle</li> <li>• Extra Practice Guide</li> <li>• Transition Guides</li> <li>• Reteaching Guide</li> <li>• Home -to- School Connection Book</li> <li>• Online Teacher Technology Kit</li> <li>• Fact Fluency</li> <li>• Online Interactive Whiteboard Lessons</li> </ul>	<ul style="list-style-type: none"> <li>• Student Texts (A &amp; B)</li> <li>• Student Workbooks</li> <li>• Online Student Technology Kit</li> <li>• Student Interactivities</li> </ul>

## **Supplemental Resources**

### **Engage NY**

[http://www.engageny.org/video-library?f\[0\]=im field subject%3A19](http://www.engageny.org/video-library?f[0]=im field subject%3A19)

### **Common Core Tools**

<http://commoncoretools.me/>

<http://www.ccsstoolbox.com/>

<http://www.achievethecore.org/steal-these-tools>

### **Achieve the Core**

<http://achievethecore.org/dashboard/300/search/6/1/0/1/2/3/4/5/6/7/8/9/10/11/12>

### **Manipulatives**

<http://nlvm.usu.edu/en/nav/vlibrary.html>

<http://www.explorelearning.com/index.cfm?method=cResource.dspBrowseCorrelations&v=s&id=USA-000>

<http://www.thinkingblocks.com/>

**Illustrative Math Project** : <http://illustrativemathematics.org/standards/k8>

**Inside Mathematics**: <http://www.insidemathematics.org/index.php/tools-for-teachers>

**Sample Balance Math Tasks**: <http://www.nottingham.ac.uk/~ttzedweb/MARS/tasks/>

**Georgia Department of Education**: <https://www.georgiastandards.org/Common-Core/Pages/Math-K-5.aspx>